

2019

PHYSICS

(Honours)

Paper : PHYII-DC - 1

[CBCS]

Full Marks : 25

Time : Two Hours

The figures in the margin indicate full marks.

Candidates are required to give their answers

in their own words as far as practicable.

I. Answer any five questions from the following :

2×5=10

(a) Show that the field $\vec{F} = \hat{i}(2xy + z^2) + \hat{j}x^2 + \hat{k}(2xz)$ is conservative.

(b) Solve the following simultaneous equations :

$$\frac{dx}{dt} = -wy \quad \text{and} \quad \frac{dy}{dt} = wx$$

(c) With the help of divergence theorem, show that

$$\int (\vec{\nabla}\phi \times \vec{\nabla}\psi) \cdot d\vec{s} = 0$$

P.T.O.

(d) Evaluate the integral $I = \int_0^2 x^2 \delta(2x-1) dx$.

(e) Find out a unit vector perpendicular to the surface $x^2 + y^2 - z^2 = 11$ at the point (4, 2, 3).

(f) Comment on the homogeneity of the differential equation $ayxe^{x/y} dx + (y - axe^{x/y}) dy = 0$.

(g) Define polar and axial vectors. Give example of each.

(h) If $u(x, y) = \tan^{-1} \frac{y}{x}$, then find $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2}$.

2. Answer any *three* questions from the following :

5×3=15

(a) Verify Gauss's divergence theorem for the vector $\vec{A} = 4xz\hat{i} - y^2\hat{j} + yz\hat{k}$ w.r.t. a unit cube with two opposite corners at (0,0,0) and (1,1,1). 5

(b) (i) Given : $A = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$,

diagonalise A .

(3)

(ii) Find a similarity transformation matrix B which diagonalises A . 2+3=5

(c) Express $\vec{\nabla}$ in spherical polar coordinates and determine $\vec{\nabla}\psi(r, \theta, \phi)$ where $\psi(r, \theta, \phi) = 2r \sin\theta + r^2 \cos\phi$. 3+2=5

(d) (i) Evaluate the integral $\int x^2 y dV$ where V is the closed region bounded by the planes $4x + 2y + z = 8$, $x = 0$, $y = 0$ and $z = 0$.

(ii) Solve $\frac{d^2 y}{dx^2} + 2\frac{dy}{dx} + y = 0$ 3½+1½=5

(e) Solve the following equation :

$$\frac{d^2 y}{dx^2} - y = x^2 \cos(x)$$

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